



Theories, Systems and Applications

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Argumentation in AI = *Machine* arguing =
design and build *machines* that argue

- to resolve conflicts (within and across)
- to reason with incomplete information
- to explain

- ① Abstract Argumentation (AA) frameworks = “webs of disagreement”
 - Semantics via extensions, labellings
- ② Structured Argumentation = arguments have structure
 - Assumption-based Argumentation (ABA)
- ③ Bipolar Argumentation (BA) frameworks = AA + support
 - deductive and necessary support, bipolar ABA, gradual semantics
- ④ Argumentation with Preferences
 - AA with preferences (delete/reverse attacks)
 - (ABA+ = ABA with preferences via reverse attack)
- ⑤ Argumentation with Probabilities
 - probabilistic AA
 - (PABA = probabilistic ABA)

- 1 AA frameworks = “webs of disagreement”
 - ArgTeach (labellings)
- 2 ABA frameworks = arguments have structure
 - ABAPlus (for **flat** ABA frameworks (with preferences))
- 3 BA frameworks = AA + support
 - Arg&Dec (gradual semantics)

An example: non-monotonic, defeasible reasoning

Am I eligible to claim for UK & European Breakdown & Recovery Assistance?

You need to think about whether the insurance meets your needs and whether you can claim when you need to.

| You are covered for: | You are not covered for: |
|--|--|
| <ul style="list-style-type: none">✓ UK and European Breakdown Assistance for account holder(s) in any private car that they are travelling in✓ Anyone driving a private car registered to the account holder and which is being used with his/her permission. Where the account is in joint names then up to 2 private cars can be covered✓ Assistance provided at home and on the roadside with national recovery and onward travel✓ No call out limit✓ No excess payable | <ul style="list-style-type: none">• The cost of replacement parts and associated labour to repair the vehicle• Private cars not registered to the account holder(s) unless the account holder(s) are in the vehicle at the time of the breakdown• Motorcycles, motorhomes, caravanettes, commercial vehicles (all types), vans, pick up trucks and vehicles being used for hire and reward purposes (such as taxis)• Vehicles that do not have a valid MOT or are not serviced or maintained in line with manufacturer guidelines• Vehicles that are more than 7 metres in length, 2.3 metres wide, 3 metres high and weigh more than 3.5 tonnes when fully loaded |



Argumentation/AA for the example: intuition

COVERED FOR: UK/EU Breakdown Assistance for account holder(s) in any private car they are travelling in

NOT COVERED FOR: private cars not registered to the account holder(s) unless in the vehicle at the time of the breakdown

Mary: account holder traveling in friend's car; car breaks down

- there is an **argument** $c(mary)$ for Mary covered (as travelling in private car)
- there is an objection (**attack**) against this argument, by an **argument** $nc(mary)$ for Mary not covered (as car not registered to Mary)
- there is an objection (**attack**) against this argument, by an **argument** $in(mary)$ for Mary in car at time of breakdown

$in(mary)$, $c(mary)$ are (dialectically) “good”;
 $in(mary)$ is (dialectically) “strongest”.

$\langle \text{Args}, \text{attacks} \rangle$ where

- Args is a set (the *arguments*)
- $\text{attacks} \subseteq \text{Args} \times \text{Args}$ is a binary relation over Args

An AA framework can be represented as a directed graph

Example

$c(\text{mary}) \longleftarrow nc(\text{mary}) \longleftarrow in(\text{mary})$

Notation

- “ α attacks β ” stands for $(\alpha, \beta) \in \text{attacks}$
- $A \subseteq \text{Args}$ attacks $B \subseteq \text{Args}$ iff there are $\alpha \in A, \beta \in B$ such that α attacks β
- $A \subseteq \text{Args}$ attacks $\beta \in \text{Args}$ iff A attacks $\{\beta\}$

“Recipes” for determining “good” sets of arguments (*extensions*)

$A \subseteq Args$ is

- **conflict-free** (c-f) iff it does not attack itself
- **admissible** iff it is c-f and attacks each attacking argument
- **preferred** iff it is maximal (wrt \subseteq) admissible
- **complete** iff it is admissible and contains all arguments it *defends* (by attacking all attacks against them)
- **stable** iff it is c-f and attacks each argument not in it

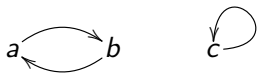
Example

$c(mary) \leftarrow nc(mary) \leftarrow in(mary)$

$\{nc(mary)\}$ is conflict-free, $\{c(mary), nc(mary)\}$ is not

$\{in(mary)\}$ is admissible, $\{nc(mary)\}$ is not

$\{c(mary), in(mary)\}$ is preferred/complete/stable, $\{in(mary)\}$ is not



- no stable extension
- two preferred extensions: $\{a\}$ and $\{b\}$
- three complete extensions: $\{\}$, $\{a\}$ and $\{b\}$

(more) Semantics for AA

“Recipes” for determining “good” sets of arguments (*extensions*)

$A \subseteq \text{Args}$ is

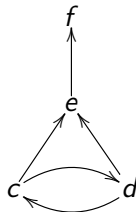
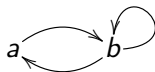
- **grounded** iff it is minimally (wrt \subseteq) complete;
- **sceptically preferred** iff it is the intersection of all preferred extensions;
- **ideal** iff it is maximal (wrt \subseteq) such that
 - (i) it is admissible and
 - (ii) it is contained in all preferred extensions

Example

$c(\text{mary}) \leftarrow nc(\text{mary}) \leftarrow in(\text{mary})$

$\{c(\text{mary}), in(\text{mary})\}$ is grounded/sceptically preferred/ideal, $\{\}$ is not

Semantics for AA: (more) differences



- grounded extension: $\{\}$
- ideal extension: $\{a\}$
- sceptically preferred extension: $\{a, f\}$

Credulous vs sceptical semantics

Credulous semantics

Possibly several alternative “good” extensions:
admissible, preferred, complete, stable

Sceptical semantics

One single “good” extension (taking no chances):
grounded, ideal, sceptically preferred



- semantics via extensions = sets of “winning” arguments
- semantics via labellings = “winning” (IN), “losing” (OUT), or “undecided” (UNDEC) arguments

in one-to-one correspondence!

Example: Complete Labelling

For every argument $\alpha \in \text{Args}$:

- ① α is labelled IN iff every argument attacking α is labelled OUT.
 - ② α is labelled OUT iff some argument attacking α is labelled IN.
- $\Rightarrow \alpha$ is labelled UNDEC iff at least one attacker of α is labelled UNDEC and no attacker is labelled IN.

- ArgTeach (<http://argteach.herokuapp.com/>)

Arguments and attacks can be obtained from other “information”

Argument have a structure - normally premises and claim

Attacks are directed - normally - at premises or claims of arguments

- ABA
- ASPIC(+)
- DeLP
- Deductive argumentation

An ABA framework is a tuple $\langle \mathcal{L}, \mathcal{R}, \mathcal{A}, \bar{\cdot} \rangle$ where

- $\langle \mathcal{L}, \mathcal{R} \rangle$ is a deductive system, with \mathcal{L} the **language** and \mathcal{R} a set of **rules**, that we assume of the form $\sigma_0 \leftarrow \sigma_1, \dots, \sigma_m (m \geq 0)$ with $\sigma_i \in \mathcal{L} (i = 0, \dots, m)$;
- $\mathcal{A} \subseteq \mathcal{L}$ is a (non-empty) set, referred to as **assumptions**;
- $\bar{\cdot}$ is a total mapping from \mathcal{A} into \mathcal{L} ; \bar{a} is referred to as the **contrary** of a .

An ABA framework is *flat* if no assumption is the head of a rule.

A possible ABA framework for UK/EU Breakdown Assistance

COVERED FOR: UK/EU Breakdown Assistance for account holder(s) in any private car they are travelling in

NOT COVERED FOR: private cars not registered to the account holder(s) unless in the vehicle at the time of the breakdown

Mary (m): account holder traveling in friend's car (c); car breaks down

rules \mathcal{R} :

$$\begin{aligned} cov(m, c) &\leftarrow ah(m), tr(m, c), pr(c), not \neg cov(m, c) \\ \neg cov(m, c) &\leftarrow \neg reg(c, m), not cov'(m, c) \\ cov'(m, c) &\leftarrow in(m, c) \\ ah(m) &\leftarrow \quad tr(m, c) \leftarrow \quad pr(c) \leftarrow \\ \neg reg(c, m) &\leftarrow \quad in(m, c) \leftarrow \end{aligned}$$

language \mathcal{L} : Herbrand base of \mathcal{R} plus (all) NAF literals

assumptions \mathcal{A} : (all) NAF literals

contrary $\overline{not\ x} = x$ for all x in the Herbrand base of \mathcal{R}

Arguments and Attacks in flat ABA

Arguments are deductions of claims using rules and supported by sets of assumptions:

- *an argument for (the claim) $\sigma \in \mathcal{L}$ supported by $A \subseteq \mathcal{A}$ ($A \vdash \sigma$ in short) is a deduction for σ supported by A (and some $R \subseteq \mathcal{R}$)*

Attacks are directed at the assumptions in the support of arguments:

- *an argument $A_1 \vdash \sigma_1$ attacks an argument $A_2 \vdash \sigma_2$ iff σ_1 is the contrary of one of the assumptions in A_2 .*

Equivalently: (“good”) extensions as sets of assumptions

- *a set of assumptions A attacks a set of assumptions A' iff an argument supported by a subset of A (possibly the full A) attacks an argument supported by a subset of A' (possibly the full A').*

(“Good”) Extensions in ABA: hands on

- ABAPLus: <http://www-abaplus.doc.ic.ac.uk/>

An example: online reviews



The Handmaid's Tale

by Margaret Atwood (Goodreads Author)

★★★★★ 4.09 · Rating details · 928,857 Ratings · 50,360 Reviews

Offred is a Handmaid in the Republic of Gilead. She may leave the home of the Commander and his wife once a day to walk to food markets whose signs are now pictures instead of words because women are no longer allowed to read. She must lie on her back once a month and pray that the Commander makes her pregnant, because in an age of declining births, Offred and the other Ha ...[more](#)

goodreads



Emily May rated it ★★★★★

Dec 05, 2010

Shelves: dystopia-utopia, favourites, feminism



“Don't let the bastards grind you down.”

There are only a small handful of books that have affected me in a REALLY personal way. In a way that I always try to put into words and always,



Victoria rated it ★★☆☆☆ · review of another edition

Jun 07, 2007

Shelves: fiction, sf-f, 2005

Not a very well written book. The writing itself is clumsy. It doesn't feel like you're reading a story; it feels like you're reading a piece of writing. Good

Bipolar Argumentation (BA)

A BA framework is $\langle \text{Args}, \text{attacks}, \text{supports} \rangle$ where

- $\langle \text{Args}, \text{attacks} \rangle$ is an AA framework
- $\text{supports} \subseteq \text{Args} \times \text{Args}$ is a binary relation over Args

A BA framework can be represented as a (directed) graph (with two types of edges)

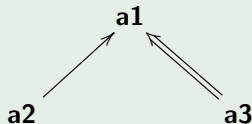
“ α supports β ” stands for $(\alpha, \beta) \in \text{supports}$

Example (Online reviews)

Read “The Handmaid’s tale” (**a1**)

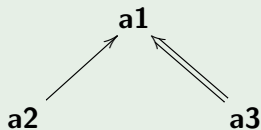
I disagree, not well written! (**a2**)

Very few books have affected me ... (**a3**)



Various notions of “good” extensions by forming *coalitions* of arguments in “support chains”

Example (Online reviews)



$\{\mathbf{a1}, \mathbf{a3}\}$ is a coalition
a2 belongs to a “good” extension

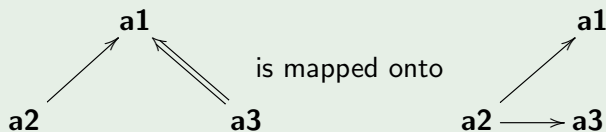
Several approaches, including:

- 1 BA frameworks where support is interpreted as *deductive*
- 2 BA frameworks where support is interpreted as *necessary* (Argumentation frameworks with necessities)

BA frameworks with deductive support

Idea: BA frameworks are first mapped onto AA frameworks, and then standard semantics are used

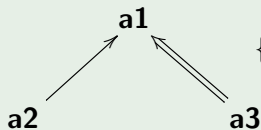
Example (Online reviews)



Argumentation frameworks with necessities (AFNs)

An AFN is a BA framework $\langle \text{Args}, \text{attacks}, \text{supports} \rangle$ where *supports* is irreflexive and transitive.

Example (Online reviews)



$\{\}, \{a2\}, \{a3\}, \{a2, a3\}$ are admissible
 $\{a2, a3\}$ is preferred/stable

An ABA framework $\langle \mathcal{L}, \mathcal{R}, \mathcal{A}, \overline{} \rangle$ is *bipolar* iff

every rule in \mathcal{R} is of the form $\varphi \leftarrow \alpha$, where $\alpha \in \mathcal{A}$ and either $\varphi \in \mathcal{A}$ or $\varphi = \overline{\beta}$ for some $\beta \in \mathcal{A}$.

Thus a bipolar ABA framework may be *non-flat*.

$E \subseteq \mathcal{A}$ is *admissible* iff

E is “closed”, conflict-free and E attacks every “closed” $A \subseteq \mathcal{A}$ attacking E .

$E \subseteq \mathcal{A}$ is *set-stable* iff

E is “closed”, conflict-free and E attacks the closure of $\{\alpha\}$ for every $\alpha \in \mathcal{A} \setminus E$.

Deductive and necessary support in ABA

The *d*-ABA framework corresponding to BA framework with deductive support is $\langle \mathcal{L}, \mathcal{R}, \mathcal{A}, \bar{\ } \rangle$ with:

- $\mathcal{L} = \text{Args} \cup \{a^c \mid a \in \text{Args}\},$
- $\mathcal{R} = \{b^c \leftarrow a \mid a \text{ attacks } b\} \cup \{b \leftarrow a \mid a \text{ supports } b\},$
- $\mathcal{A} = \text{Args},$
- $\bar{a} = a^c \quad \forall a \in \mathcal{A}.$

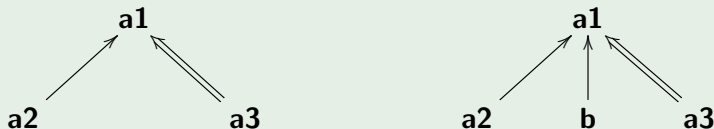
The *n*-ABA framework corresponding to AFN is $\langle \mathcal{L}, \mathcal{R}, \mathcal{A}, \bar{\ } \rangle$ with:

- $\mathcal{L} = \text{Args} \cup \{a^c \mid a \in \text{Args}\},$
- $\mathcal{R} = \{b^c \leftarrow a \mid a \text{ attacks } b\} \cup \{a \leftarrow b \mid a \text{ supports } b\},$
- $\mathcal{A} = \text{Args},$
- $\bar{a} = a^c \quad \forall a \in \mathcal{A}.$

Considerations on deductive vs necessary support

- they sanction different extensions as “good”
- they are useful in different contexts:
 - *evidence supports fact*: deductive interpretation
(e.g. a reputable news distributor says X *supports* X holds)
 - *motive supports evidence*: necessary interpretation
(e.g. politician has motive to say X *supports* politician says X)
- as in AA, neither semantics **accrue** (accrual=“the fact of something increasing over a period of time”), e.g.:

Example (Online reviews)



{a1} equally not “good”

Gradual semantics for arguments: accrual

| Semantics | Choices | | | | | Principles | | | |
|---------------------------|---------|----------------|--------|------------------|-------------------|------------|----|---|----|
| | QBAF | \mathbb{I} | τ | * | \ll | B | SB | M | SM |
| h-Categorizer | aQBAF | $(0, 1]$ | 1 | σ_{\perp} | $<$ | ✓ | ✓ | ✓ | ✓ |
| Inverse Equational System | aQBAF | $[0, 1]$ | 1 | σ_{\perp} | $<_0$ | ✓ | ✓ | ✓ | ✓ |
| Suspect Equational System | aQBAF | $[0, 1]$ | 1 | σ_{\perp} | $<_0$ | ✓ | . | . | . |
| Max Equational System | aQBAF | $[0, 1]$ | 1 | σ_{\perp} | $<$ | ✓ | ✓ | ✓ | . |
| GTAA | aQBAF | $[0, 1]$ | 1 | σ_{\perp} | $<$ | ✓ | ✓ | . | . |
| GTBA | QBAF | $[0, 1]$ | 0.5 | - | - | . | . | . | . |
| LocMax | QBAF | $[-1, 1]$ | 0 | σ_{\perp} | $<_0$ | ✓ | . | ✓ | . |
| LocSum | QBAF | $[-1, 1]$ | 0 | σ_{\perp} | $<$ | ✓ | . | ✓ | ✓ |
| Social Models | aQBAF | ordered set | - | σ_{\perp} | $<$ | ✓ | ✓ | ✓ | ✓ |
| Weighted Max-Based | aQBAF | $[0, 1]$ | - | σ_{\perp} | $<$ | ✓ | ✓ | ✓ | . |
| Weighted Card-Based | aQBAF | $[0, 1]$ | - | σ_{\perp} | $<$ | ✓ | ✓ | ✓ | ✓ |
| Weighted h-Categorizer | aQBAF | $[0, 1]$ | - | σ_{\perp} | $<$ | ✓ | ✓ | ✓ | ✓ |
| Top-Based Support | sQBAF | $[0, 1]$ | - | σ_{\perp} | $<_{\tau}$ | ✓ | ✓ | ✓ | . |
| Reward-Based Support | sQBAF | $[0, 1]$ | - | σ_{\perp} | $<_{\tau}$ | ✓ | ✓ | ✓ | ✓ |
| Aggregation-Based Support | sQBAF | $[0, 1]$ | - | σ_{\perp} | $<_{\tau}$ | ✓ | ✓ | ✓ | ✓ |
| QuAD | QBAF | $[0, 1]$ | - | σ_{\perp} | - | . | . | ✓ | . |
| DF-QuAD | QBAF | $[0, 1]$ | - | σ_{\perp} | \leq | ✓ | . | ✓ | . |
| Restricted Euler-based | QBAF | $[0, 1]$ | - | σ_{\perp} | $<_{\perp, \tau}$ | ✓ | . | ✓ | ✓ |
| Complete Labellings | aQBAF | {in, out, und} | in | σ_{\perp} | $<$ | ✓ | ✓ | ✓ | . |

Gradual semantics for arguments: DF-QuAD

Given a *BA* (tree) framework $\langle \text{Args}, \text{attacks}, \text{supports} \rangle$

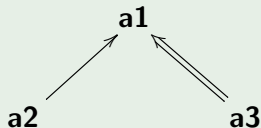
and a *base score* for arguments $\mathcal{BS} : \text{Args} \rightarrow [0, 1]$

determine the *strength* of arguments $\mathcal{S} : \text{Args} \rightarrow [0, 1]$

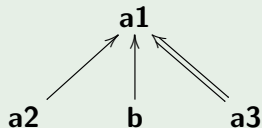
by **aggregating**

the strengths of attackers against and the strengths of supporters for these arguments

Example (Online reviews (for all $\alpha \in \text{Args} : \mathcal{BS}(\alpha) = 0.5$) - DF-QuAD)



$$\mathcal{S}(\mathbf{a1}) = 0.5$$



$$\mathcal{S}(\mathbf{a1}) = 0.375$$

DF-QuAD: effect of base score

Given a *BA* (tree) framework $\langle \text{Args}, \text{attacks}, \text{supports} \rangle$

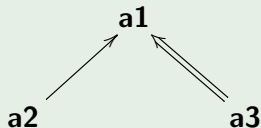
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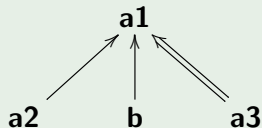
by **aggregating**

the strengths of attackers against and the strengths of supporters for these arguments

Example (Online reviews ($\mathcal{BS}(a1) = \mathcal{BS}(a3) = \mathcal{BS}(b) = 0.5$,
 $\mathcal{BS}(a2) = 0.9$) - DF-QuAD)



$$\mathcal{S}(a1) = 0.3$$



$$\mathcal{S}(a1) = 0.275$$

Arg&Dec (www.arganddec.com)

Example

R : The Economist: Remain

L : The Daily Mail: Leave

The Economist is more trustworthy than The Daily Mail

- $Args = \{R, L\}$
- $attacks = \{(L, R), (R, L)\}$ $R \longleftrightarrow L$
- $L < R$ (L is less preferred than R)

Ignoring preference:

- grounded/ideal extension: $\{\}$;
- stable/preferred extensions: $\{R\}$ and $\{L\}$.

Taking preferences into account:

- intuitively accept (only) $\{R\}$. How? Modify *attacks*

AA with Preferences: Deleting Attacks

An *AA framework with preferences* (AAP framework) is $\langle \text{Args}, \text{attacks}, < \rangle$ where

- $\langle \text{Args}, \text{attacks} \rangle$ is an AA framework
- $<$ is a transitive binary (*preference*) relation on *Args*

An AAP framework yields an AA framework $\langle \text{Args}, \text{attacks}' \rangle$ where

- $(\alpha, \beta) \in \text{attacks}'$ iff $(\alpha, \beta) \in \text{attacks}$ and $\alpha \not< \beta$.

Extensions of $\langle \text{Args}, \text{attacks}, < \rangle$ are extensions of $\langle \text{Args}, \text{attacks}' \rangle$

Example

$R \longleftrightarrow L$ with $L < R$ yields $R \longrightarrow L$

AA with Preferences: Reversing Attacks

An *AA framework with preferences* (AAP framework) is $\langle \text{Args}, \text{attacks}, < \rangle$ where

- $\langle \text{Args}, \text{attacks} \rangle$ is an AA framework
- $<$ is a transitive binary (*preference*) relation on *Args*

An AAP framework yields an AA framework $\langle \text{Args}, \text{attacks}'' \rangle$ where

- $(\alpha, \beta) \in \text{attacks}''$ iff $(\alpha, \beta) \in \text{attacks}$ and $\alpha \not< \beta$ or $(\beta, \alpha) \in \text{attacks}$ and $\beta < \alpha$

Extensions of $\langle \text{Args}, \text{attacks}, < \rangle$ are extensions of $\langle \text{Args}, \text{attacks}'' \rangle$

Example

$R \longleftrightarrow L$ with $L < R$ yields $R \longrightarrow L$

preferences over “building blocks” (rules, assumptions)

- ASPIC+ : deleting attacks
- ABA+ : reversing attacks; ABAPlus:
<http://www-abaplus.doc.ic.ac.uk/>

(DeLP: preferences via specificity)

A *probabilistic AA framework* is $(\langle \text{Args}, \text{attacks} \rangle, \Pi, \vdash)$ where

- $\langle \text{Args}, \text{attacks} \rangle$ is an AA framework
- $\Pi = (\mathcal{W}, P)$ is a probability space
- $\vdash \subseteq \mathcal{W} \times \text{Args}$ specifies arguments' *applicability* in Π 's worlds

For $w \in \mathcal{W}$:

- the AA framework *w.r.t.* w is $\langle \text{Args}_w, \text{attacks}_w \rangle$ where
 $\text{Args}_w = \{ \alpha \in \text{Args} \mid w \vdash \alpha \}$
 $\text{attacks}_w = \text{attacks} \cap (\text{Args}_w \times \text{Args}_w)$
- let \mathcal{G}_w be the grounded extension of $\langle \text{Args}_w, \text{attacks}_w \rangle$; then the *grounded probability* of $\alpha \in \text{Args}$ is

$$\text{Prob}_{\mathcal{G}}(\alpha) = \sum_{w \in \mathcal{W}: \alpha \in \mathcal{G}_w} P(w).$$

probabilities over “building blocks” (assumptions)

- PABA
- <http://ict.siiit.tu.ac.th/hung/Prengine>

- (Basics of) AA, BA, Structured argumentation (flat ABA, bipolar ABA), AA with preferences, probabilistic AA
- Omissions
 - Computation
 - Properties
 - Instances
 - Dialogical Argumentation
 - ...

- P. M. Dung: On the Acceptability of Arguments and its Fundamental Role in Nonmonotonic Reasoning, Logic Programming and n-Person Games. *Artif. Intell.* 77(2): 321-358 (1995)
- P. M. Dung, P. Mancarella, F. Toni: Computing ideal sceptical argumentation. *Artif. Intell.* 171(10-15): 642-674 (2007)

- C. Cayrol and M.-C. Lagasque-Schiex: Bipolarity in argumentation graphs: Towards a better understanding. International Journal of Approximate Reasoning 2013.
- F. Nouioua and V. Risch: Argumentation Frameworks with Necessities. SUM 2011.
- A. Rago, F. Toni, M. Aurisicchio, P. Baroni: Discontinuity-Free Decision Support with Quantitative Argumentation Debates, KR 2016
- P. Baroni, A. Rago and F. Toni, How Many Properties Do We Need for Gradual Argumentation?, AAI 2018

- P. Besnard, A. Garcia, A. Hunter, S. Modgil, H. Prakken , G. Simari and F. Toni, Introduction to structured argumentation, Argument & Computation, Special Issue: Tutorials on Structured Argumentation, 2014
- F. Toni, A tutorial on assumption-based argumentation, Argument & Computation, Special Issue: Tutorials on Structured Argumentation, 2014
- K. Cyras, C. Schulz and F. Toni, Capturing Bipolar Argumentation in Non-flat Assumption-Based Argumentation, PRIMA 2017

- L. Amgoud and C. Cayrol, A Reasoning Model Based on the Production of Acceptable Arguments. *Ann. Math. Artif. Intell.*, 34(1-3):197–215
- L. Amgoud and S. Vesic, Rich Preference-Based Argumentation Frameworks. *Int. J. Approx. Reasoning*, 55(2):585–606.
- S. Modgil and H. Prakken, The ASPIC+ Framework for Structured Argumentation: A Tutorial. *Arg.&Comp.*, 5(1):31–62.
- K. Čyras and F. Toni, ABA+: Assumption-Based Argumentation with Preferences. *KR 2016*.

- P. M. Dung, P. M. Thang, Towards (Probabilistic) Argumentation for Jury-based Dispute Resolution, COMMA 2010
- N. D. Hung, Inference procedures and engine for probabilistic argumentation, International Journal of Approximate Reasoning 90, 2017